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Lanthanide-based thermometers: At the cutting-edge of luminescence thermometry

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This paper is dedicated to the memory of A. L. L. Videira who recently passed away. He was a brilliant professor and a truly extraordinary human being whose legacy will endure in all whose lives he touched.

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Abstract:
Present technological demands in disparate areas, such as micro and nanofluidics, micro and nanoelectronics, photonics and biomedicine, among others, have reached to a development such that conventional contact thermal probes are not accomplished to perform accurate measurements with submicrometric spatial resolution. The development of novel non-contact thermal probes is, then, mandatory, contributing for an expansionary epoch of luminescence thermometry. Luminescence thermometry based on trivalent lanthanide ions becomes very popular since 2010 due to the unique versatility, stability and narrow emission band profiles of the ions that cover the entire electromagnetic spectrum with relatively high emission quantum yields. Here we give a
perspective overview on the field since the beginnings in the 1950’s until the most recent cutting-edge examples. The current movement towards the technique usage as a new tool for thermal imaging, early tumor detection and as a tool for unveil properties of the thermometers themselves or of their local neighborhoods is also summarized.
1. Introduction

Temperature, termed from Latin word "temperātūra", is an intensive physical quantity measuring the internal thermal energy state of a substance.\cite{1} The statistical physics definition of temperature of a body is the inverse of the change of its entropy $S$, with respect to the internal energy $U$, $T^{-1} = \partial S/\partial U$.\cite{2,3} Whereas body’s entropy measures the amount of its atomic disorder, temperature measures the intensity of submicroscopic random movements of the body’s constituents. The precise and accurate measurement of the temperature is vital across a broad spectrum of areas, such as automotive, aerospace and defense, metrology, climate, marine research, bio and nanomedicine, electronics, heating and cooling devices, production plants, and food’s storage.\cite{4-11} Presently, temperature sensors account for ~80% of the worldwide sensor market that is expected to reach to $6.86$ billion by 2023, accordingly to the Grand View Research, Inc.\cite{12} (Figure 1).

From the invention of thermoscope by Galileo until our days, many new methods and temperature sensors have been developed.\cite{13} Generally, the temperature reading is achieved from an invasive probe material in direct physical contact with the body for which temperature is unknown. Thermocouples and thermistors dominate the market but are inappropriate below 10 μm, as the required thermal connection with the sample disturbs the measurements at those small scales.\cite{10,14-21} Furthermore, these conventional contact thermometers depend upon an electrical link hampering their applications where the electromagnetic noise is significant and sparks are dangerous.\cite{4}

Hence, such restrictions of contact thermometers for systems of small dimensions have been stimulating the development of new non-contact precise thermometers with spatial resolution at the micro and nanometric scales, an exciting research topic under continuous expansion in the last decade.\cite{16-19,21,22} High-resolution non-contact thermometers operating at those scales have been grouped using distinct criteria, as whether they make use of optical or electrical signals or they are based on near- or far-field techniques. However, each method, possesses several advantages as well as drawbacks and exhibit different spatial, temporal, and temperature resolution (see, for instance, Table 1 of ref. \cite{10} for details).

Thermographic phosphor thermometry is a noninvasive spectroscopic technique for temperature measurement based on the phosphor emission temperature dependence (e.g., peak energy and intensity, bandshape, and excited states lifetimes and risetimes). This technique
combines high relative thermal sensitivity (>1 %·K⁻¹) and spatial resolution (<10 µm) in short acquisition times (<1 ms), and, as it operates remotely, works even in biological fluids, fast-moving objects and strong electromagnetic fields. The most used method to calculate the absolute temperature through thermographic phosphor thermometry is by measuring the luminescence intensities of two electronic transitions (occasionally involving Stark components of an excited electronic state) in thermal equilibrium (see section 4). Moreover, different phosphors have been examined for providing a contactless thermal reading through their light emission properties, e.g., polymers, DNA or protein conjugated systems, organic dyes, quantum dots (QDs), Cr³⁺-based materials, and trivalent lanthanide (Ln³⁺) ions (for a recent review see ref. [10]).

Organic dyes are the most available and used thermal probes; for an exhaustive review of the subject see the works of Hoogenboom and collaborators.[33, 34] However, recently QDs and Ln³⁺-based materials are gaining importance, due to their higher photostability. For instance, QDs were employed in submicron thermometry due to its temperature-dependent luminescence features (intensity changes or emission peak shifts).[35, 36] One of the most appealing applications area for QDs is nanomedicine, since its bioconjugation can make them target selective. Nevertheless, QDs usage in future use in clinical trials may be difficult, as they generally include highly toxic elements (e.g. Cd).[37, 38] The work of Jaque and collaborators gives a complete review of the application of QDs in micro and nanothermometry.[39]

Ln³⁺-based materials are stable and narrow band emitters covering the entire electromagnetic spectrum with, in general, high emission quantum yields (>50% in the visible).[40-47] In the last decade, many Ln³⁺-based thermometers have been reported covering a wide temperature range, from cryogenic (T<100 K) to physiological (298–323 K) values, and including chelate complexes,[14, 15, 48] metal organic frameworks (MOFs),[49-52] polymers,[53, 54] organic-inorganic hybrids,[48, 55] upconverting,[56-59] downconverting[60] and downshifting[61-64] nanoparticles (NPs) and multifunctional heater-thermometer nanoplatforms.[65-67] The implementation of these Ln³⁺-based phosphors as ratiometric thermometers in diverse applications was extensively revised in the past decade,[7, 9, 10, 16-19, 21, 50, 52, 57, 68-83] including in two books.[84, 85]

The story of thermographic phosphor thermometry began in 1937 with Neubert[86, 87] during the development of the fluorescent lamp (for a review see the works of Allison and Gillies[4] and Khalid and Kontis[66]). The observed loss of luminescence intensity with increasing temperature
suggested the use of phosphor emission as a nonintrusive technique for monitoring the temperature of hot bodies. In short, the bodies were optically projected on an excited luminous screen and the temperature is rendered visible analyzing the image formed by the quenching of the luminescence of the screen produced by the infrared radiation emitted from the hot body.\textsuperscript{[86, 87]}

Twelve years later, Urbach et al. shown that the temperature-dependence of the luminescent efficiency of numerous phosphors could be used for the measurement of temperatures and temperature distributions, Figure 2.\textsuperscript{[88]} The first applications, in aeronautics and medicine, date back to the 1950’s and 1960’s. In the former example, a phosphor was painted on the wing surfaces of a wind-tunnel model in order to probe the temperature, Figure 3,\textsuperscript{[89]} while a couple of years later, and during the course of some studies on drug-induced tumor pain, it became clear that most breast cancers were characterized by an increase in temperature.\textsuperscript{[90]} This heat elevation could be detected in the skin over the tumors and Lawson et al. in 1965 reported the employment of a thermally sensitive ZnCdS-based phosphor to record the human skin temperature, opening the avenue to apply thermography to clinical diagnosis, Figure 4.\textsuperscript{[90, 91]}

After these pioneering works the interest on luminescent thermometers remains essentially flat until the 1990’s, with less than 10 publications by year, Figure 5. In this period, mention must be done to some intriguing works on Ln\textsuperscript{3+}-based luminescent thermometers\textsuperscript{[92-94]} and its applications in thermal imaging of surfaces\textsuperscript{[95, 96]} and high-speed integrated circuits\textsuperscript{[97]} and to fiber tip thermometry systems. These last systems, commonly known as fluoroptic sensors, were initially proposed by Wickersheim and Alves\textsuperscript{[98]} by applying a phosphor at the tip of an optical fiber, for a review see the work of Wickersheim and Sun.\textsuperscript{[99]} In 1978, Luxtron (now LumaSense Technologies) industrialized the idea through the creation of its Fluoroptic\textsuperscript{®} technology working through the \textsuperscript{5}D\textsubscript{0} decay time of Gd\textsubscript{2}O\textsubscript{2}S:Eu\textsuperscript{3+}.\textsuperscript{[100]} From 1995 to date, the fluoroptic sensors have been extensively used in distinct thermal invasive procedures for tumor removal,\textsuperscript{[101]} and for in vivo measurements of brain temperature.\textsuperscript{[102]} As far as we know, the fluoroptic device was the only commercial product based on luminescence thermometry until the recent launch by Edinburgh Instruments of an system coupling a commercial upconversion phosphor (NaY\textsubscript{0.77}Yb\textsubscript{0.20}Er\textsubscript{0.03}F\textsubscript{4}, Sigma Aldrich) to a temperature stage and a FLS1000 photoluminescence spectrometer.\textsuperscript{[103]}

In 2002, a major breakthrough on the subject arise with the inspiring work of Wang et al. about using luminescent NPs for thermometry.\textsuperscript{[104]} Ratiometric luminescent thermometers based on ZnS:Mn\textsuperscript{2+}, Eu\textsuperscript{3+} semiconductor NPs were introduced taking the temperature-dependent ratio of the
emission intensities of the two dopants – the so-called fluorescence intensity ratio, FIR. This concept was generalized a few years later to NPs doped exclusively with Ln$^{3+}$ ions (e.g. BaTiO$_3$:Er$^{3+}$ NPs).\textsuperscript{[105]}

The topic has then exploded around 2010 (Figure 5), particularly due to the recognition of the enormous potential of luminescence thermometry in nanotechnology and nanomedicine. A few illustrative examples of important papers dated from that period involving Ln$^{3+}$-doped materials are:

- Phonon-induced heat generation and simultaneous noncontact temperature sensing Yb$^{3+}$/Er$^{3+}$-based upconverting nanoparticles (UCNPs)\textsuperscript{[106]} and Nd$^{3+}$-based NPs;\textsuperscript{[107]}
- Intracellular thermometers using Yb$^{3+}$/Er$^{3+}$-doped UCNPs;\textsuperscript{[59, 108]}
- Eu$^{3+}$-doped organic-inorganic hybrid NPs for temperature probing in the physiological range;\textsuperscript{[48]}
- Eu$^{3+}$/Tb$^{3+}$-doped organic-inorganic hybrid thermometers, including NPs\textsuperscript{[15]} and MOFs;\textsuperscript{[109]}
- \textit{In vivo} imaging and temperature sensing using Tm$^{3+}$/Er$^{3+}$/Ho$^{3+}$-doped\textsuperscript{[110]} and poly acrylic acid- coated Mo sensitized Yb$^{3+}$/Er$^{3+}$-doped NPs.\textsuperscript{[111]}

Several reviews appeared on that explosion time (2010–2012), including examples on multiple optical chemical sensors,\textsuperscript{[112]} inorganic phosphors that can withstand extreme temperatures,\textsuperscript{[70, 113, 114]} luminescent and non-luminescent high-resolution micro and nanothermometers,\textsuperscript{[16-18, 71]} UCNPs,\textsuperscript{[72]} and temperature-stimuli polymers.\textsuperscript{[133, 115]} After this period, the number of publications and corresponding citations has continued to grow exponentially, Figure 5a,b. Intriguing examples involving Ln$^{3+}$-doped materials are \textit{in situ} measurements to visualize temperature gradients in photonic devices,\textsuperscript{[116, 117]} microelectronic\textsuperscript{[118]} and microfluidic\textsuperscript{[119]} chips, catalytic processes,\textsuperscript{[120]} dosimeters working in high-energy radiation fields,\textsuperscript{[121]} and heated air jets and internal parts of combustion engines.\textsuperscript{[122]} Currently, luminescence thermometry lives its inflationary epoch, with a total number of papers (citations) representing ~2.5% (2.0%) of the total number of papers (citations) published in the same period in the context of luminescence or luminescent systems, Figure 5c,d.

In the last couple of years, we are observing a gradually shift of the emphasis of luminescence thermometry from the synthesis and general characterization of new thermographic phosphors towards the use of the technique for thermal imaging, early tumor detection and as a tool for unveil
thermometers’ features or details of their local surroundings. In the former case, examples include recording of *in vivo* thermal images,[123-126] acquisition of subcutaneous thermal videos[125] and *in vivo* ischemia recognition in small animals.[126] Early tumor detection becomes possible by transient thermometry using NIR emitting Ag$_2$S nanocrystals.[127] Examples of the later approach are the analysis of heat flux assessment in heater-thermometer nanoplatforms,[128] the estimation of the absorption coefficient and of the thermal diffusivity of tissues,[129] the quantification of the instantaneous ballistic velocity of Brownian nanocrystals suspended in aqueous and organic solvents,[130] the determination of the thermal conductivity of porous silica and titania nanostructures,[131] and the measurement of the thermal resistance of NPs (in air).[132] Among these recent examples, the present manuscript considers essentially those based on Ln$^{3+}$ ions, being a follow up of the two books[84, 85] and the review papers published since 2015 on Ln$^{3+}$-based luminescent thermometers.[9, 10, 16-19, 21, 50, 52, 74, 79, 80, 82, 83] The few examples involving other emitting centers are included in the text either in the context of historical reasons, e.g. the ZnCdS-based phosphors,[88-91] or due to its enormous impact for the development of the area, e.g. the Ag$_2$S nanocrystals.[127]

2. **Classifying thermometers: Primary and secondary thermometers**

There are many ways of sorting thermometers. Here, we list the most used classification regarding the way how the sensor is in physical contact with the probe and the intensity-to-temperature calibration relation.

Concerning the physical interaction between the thermal probe and the measurand, the thermometers can be classified as contact (evasive, e.g. thermocouples and thermistors) or non-contact (minimally evasive, e.g. infrared pyrometers). In between, semi-invasive thermometers are those in which there is contact between the sample and the probe, but the temperature is remotely interrogated. While the contact thermometers are well-suited for routine punctual measurements of non-moving systems, non-contact examples are appropriate for temperature measurements or mappings on moving objects or on objects in hazardous locations (e.g. thermal inspection of devices). The suitability of a given thermometer for an application is related to its sensing performance (e.g. operating range, thermal sensitivity, temperature uncertainty, acquisition rate, and spatio-temporal resolution), but also with the material’s properties (e.g. physical state, simple and easy processable synthesis, facility to be implemented, and mechanical and thermal stability).
Contact thermal characterization methods for small scales applied to active and passive devices and interconnects were reviewed by Christofferson et al.\textsuperscript{[133]}

Depending on the calibration relation, the temperature probes can be classified into primary and secondary thermometers. While the temperature is determined based on the knowledge of thermodynamic laws and quantities the thermometer is termed as primary. Contrary, if the temperature is calculated via comparison with a reference thermal probe, a calibration process is required and the thermometer is labeled as secondary.\textsuperscript{[134]} Basically, whenever the knowledge of a measurable physical quantity is not enough to calculate the temperature from an equation of state (relating temperature with other measurable physical quantities), the thermometer must be referred to an external temperature reference and it is called secondary.

Up to know, five thermodynamic measurable quantities are used to determine temperature in primary thermometry: the pressure of a gas in a constant volume, the speed of sound in a monatomic gas, the dielectric constant of a gas, the black-body emission, and the power spectral density of Johnson-noise in an electrical resistor.\textsuperscript{[134,135]} Moreover, although primary thermometers are generally complex and mostly employed for metrology purposes, they are currently engaged in the redefinition of the international temperature scale (1990’s International Temperature Scale or ITS-90) in terms of the Boltzmann constant (\(k_B\)).\textsuperscript{[136]}

Examples of primary luminescent thermometers are, however, very scarce. Up to now, the reported examples are based on CdSe(ZnS) QDs,\textsuperscript{[137]} Si NPs functionalized with 1-dodecene,\textsuperscript{[138]} \(\text{Y}_2\text{O}_3:\text{Eu}^{3+}\) micro- and nanoparticles,\textsuperscript{[139]} and \(\text{SrF}_2:\text{Yb}^{3+}/\text{Er}^{3+}\) UCNPs.\textsuperscript{[140]} This last work, discussed in detail in section 4.1.1, is based on the Boltzmann law as the equation of state and is a major breakthrough on the subject. It demonstrates that any luminescent thermometer based on a ratio of intensities arising from two thermally-coupled emitting levels can be used to determine the temperature without a previous calibration procedure.

The most known secondary thermometers are electrical probes, such as platinum resistance thermometers, thermocouples, thermistors, capacitance thermometers and silicon diodes.\textsuperscript{[57]} Although in general secondary thermometers are less complex than primary ones, recurrent calibrations are required, namely when the thermometers are used in a medium different than the one in which they were calibrated. This is a tedious and time-consuming task that is not always possible to be executed for luminescent thermometers, as, for instance, in living cells and in operating electronic devices. Indeed, many of the secondary thermometers reported in the literature
assume valid a unique calibration relation, independent of the medium, a procedure potentially inaccurate (see section 4.1.1).

3. Thermometers’ performance

The quantitative comparison of the performance of any temperature probe is critical to evaluate its use and for the comparison between distinct techniques. Thermometers’ performance can be evaluated based on its relative thermal sensitivity, temperature uncertainty, repeatability, reproducibility and spatio-temporal resolution. All the performance parameters for luminescent thermometers were recently reviewed[10] and, then, in what follows we only present a short summary highlighting the most important aspects. Table 1 summarizes the relative thermal sensitivity and temperature uncertainty values (including the working temperature and spectral ranges) of illustrative examples of the distinct classes of Ln$^{3+}$-based luminescent thermometers discussed in the review.

3.1. Thermal sensitivity

The thermal sensitivity is the rate of change of the thermometric parameter (generally, designated by $\Delta$), in response to the variation of temperature. The absolute thermal sensitivity ($S_a$) is expressed as:[141]

$$S_a = \frac{\partial \Delta}{\partial T}$$

(1)

depending only on the degree of the thermally-induced variations in $\Delta$. However, it is meaningless to quantitatively compare the thermal sensitivity among thermometers of different nature operating by different physical principles (e.g. optical, electrical, or mechanical thermometers) or, using the same physical principle, operate using different materials. To compare the performance of distinct thermometers, irrespectively of their nature or the material employed, the relative thermal sensitivity ($S_r$) should be adopted:

$$S_r = \frac{1}{\Delta} \left| \frac{\partial \Delta}{\partial T} \right|.$$ 

(2)
This parameter was introduced in 1998 by Collins et al.,\textsuperscript{141} and has been extensively adopted as a figure of merit for the comparison of the thermometers’ performance after the proposal of Brites et al. in 2012.\textsuperscript{17} $S_r$ is usually expressed in units of % change per degree of temperature change (\%/K$^{-1}$), being the maximum value of $S_r$ denoted by $S_m$ (occurring at a temperature designated as $T_m$).\textsuperscript{10}

### 3.2. Temperature uncertainty

The temperature uncertainty (or temperature resolution) $\delta T$ describes the smallest temperature resolvable by the thermometer, depending not only on the material but also on the experimental setup used. The uncertainty in the temperature arise from several factors, such as the experimental detection setup, the acquisition conditions, and the signal-to-noise ratio. Usually, $\delta T$ is estimated by the time-dependent output fluctuations of the thermometer calculating the evolution of the temporal fluctuations on the thermometric parameter. Using a calibration curve, the temperature that corresponds to each $\Delta$ is obtained (calculated from an equation of state in primary thermometers or empirically obtained in secondary examples), allowing the construction of a histogram of the temperature readouts during a certain time interval. The experimental $\delta T$ of the thermometer is the standard deviation of the resulting temperature histogram. When this strategy is not possible to be implemented, an estimate of the temperature uncertainty is given by:\textsuperscript{10}

$$\delta T = \frac{1}{S_r} \frac{\delta \Delta}{\Delta}$$

where $\delta \Delta/\Delta$ is the relative uncertainty in the determination of the thermometric parameter (depending on the acquisition setup and estimated from the errors in $\Delta$). This value is controlled adjusting the signal-to-noise ratio of the emission spectrum used to calculate each $\Delta$ value, \textit{e.g.} larger integration times and/or averaging consecutive measurements. Clearly, there is a compromise between dropping $\delta T$ and increasing the acquisition time. In fact, the longer is the acquisition time, the lower is the temperature uncertainty, resulting the minimum $\delta T$ value from the temperatures histogram’s standard deviation in the limit $t \to \infty$. 

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\textsuperscript{141} Collins, J. et al., 1998.

\textsuperscript{17} Brites, D. et al., 2012.
One interesting strategy to quantify the minimum temperature uncertainty of any thermometer was reported by Alicki et al. applying the spin-boson model and using size and system-dependent properties.\cite{142} For solid-state nanothermometers, the relative fluctuation in temperature is related to the number of atoms in the sample ($N_A$) and its Debye temperature ($T_D$):

$$\delta T = \left( \frac{4T_D^3}{3\sqrt{3} \sqrt{T_D}} e^{\frac{3T_D}{8T}} \right) \frac{1}{\sqrt{N_A}} T. \tag{4}$$

For $T_D$ in the range 100 to 2000 K the term in parenthesis changes between 0.9 and 1.3, meaning that the order of magnitude of the temperature uncertainty is determined by:\cite{142}

$$\delta T \sim \frac{T}{\sqrt{N_A}} \tag{5}$$

which means that the minimum achievable $\delta T$ is fundamentally controlled by the size of the thermal probe. In quantum metrology it is known that for non-entangled particles the precision $\theta$ of a general quantity $\theta$ scales with the inverse of the number of particles ($N_P$):\cite{143}

$$\delta \theta \sim \frac{1}{\sqrt{N_P}} \tag{6}$$

a relation called shot-noise scaling (for entangled states, however, Heisenberg-scaling applies and $\delta \theta$ is inversely proportional to $N_P$). As $N_P$ is proportional to $N_A$, Eq. 6 supports the result of the model derived by Alicki et al.\cite{142} (Eq. 5).

There are very few examples reporting the thermal resolution of luminescent thermometers as a function of its size. One case is Alaulamie’s work\cite{144} that examined experimentally the correlation between particle size and the temperature uncertainty based on the temperature readouts of Er$^{3+}$-doped UCNPs clusters of different sizes (ranging from 1 to 9 μm). Briefly, the larger the cluster size the higher the signal-to-noise ratio, leading to smaller temperature uncertainties (low standard deviation value). The experimental data present an unequivocal increase of the temperature uncertainty as the cluster size decreases, in accord with Eq. 5 and Eq.
6. For the examples discussed below in section 5.2.1 for which $S_r$ increases as the size of the crystals decreases, Eq. 3 and Eq. 5 are only compatible if the decrease in $1/S_r$ is less than the increment of $\Delta V/\Delta$, resulting in an overall increase of $\delta T$ with the decrease of $N_A$.

**3.3. Resolution, reproducibility and repeatability**

The spatial ($\delta x$) and temporal ($\delta t$) resolution of a measurement are defined as the minimum distance or time interval between measurements, respectively, presenting a temperature change larger than $\delta T$.

The thermometer’s reproducibility is the change of the same measurement carried out under modified circumstances (e.g. different equipment in use, different measurement methods, different observers, etc.).

The repeatability, $R$, describes the thermometer ability to provide repeatedly the same result, under the same circumstances and is computed by:

$$R = 1 - \frac{\max|\Delta_c - \Delta_i|}{\Delta_c}$$

(7)

where $\Delta_c$ and $\Delta_i$ represent, respectively, the thermometric parameter’s mean value and the thermometric parameter measured at each temperature.

**4. Sensing temperature with luminescence**

Luminescence is affected by the temperature, among other external stimuli, and the induced changes can be monitored measuring distinct parameters of the emitting center, such as (i) the integrated emission intensity of a single transition or of a pair of transitions, (ii) the spectral shift, bandshape or bandwidth of a given transition, and (iii) lifetime measurements, using the time-decay intensity profiles of emitting excited states (Figure 6). As the emission properties are characteristic of the emitting center itself, no fundamental limitations preclude the development of thermal probes with nanometric size. Luminescence thermometry exploits those emission temperature-induced changes either following the spectral changes of a given emission spectra (time-integrated scheme) or the temporal changes of a given transition (time-resolved scheme), as detailed in the next two sections.
It must be pointed out that when the thermometric parameter $\Delta$ is calculated based on integrated intensities, spectral shifts or bandwidths, the emission spectra must be represented as a function of energy and not wavelength, to circumvent misleading and incorrect conclusions. For this (and besides the normal correction for the instrumental response of the equipment), the photon flux per constant wavelength interval function, $\phi(\lambda)$, must be converted to photon flux per energy interval, $\phi(E)$, accordingly to:

\[
\phi(E) = \frac{d\phi(\lambda)}{dE} = \frac{d\phi(\lambda)}{dE} \left(\frac{hc}{E}\right) = -\phi(\lambda) \frac{hc}{E^2}
\]

where $h$ is the Planck constant, $c$ is the speed of the light, and the minus sign – that can be ignored – simply indicates the distinct directions of integration in $\lambda$ and $E$. This correction (known as Jacobian transformation) was seldom performed in the field of luminescence thermometry (in fact, more generally in luminescence spectroscopy) but can be critical, especially when the spectrum displays multiple peaks over a wide energy range and with different bandwidths.\[^{145,146}\] Despite the Jacobian transformation will have little effect on $4f$ transitions, especially when those enrolled in the calculus of $\Delta$ are closely-spaced, its usage is strongly encouraged for an exact description of the materials’ electronic structure and a proper evaluation of the thermometers’ performance.

### 4.1. Time-integrated schemes

Generally, the emission intensity of a given transition is sensitive to temperature changes due to the following mechanisms:

- Population redistribution over electronic levels accordingly to the Boltzmann statistics;
- Temperature-activated quenching mechanisms *(e.g. cross-relaxation between electronic levels)*;
- Non-radiative deactivations *(the electrons relax from excited states to the ground state generating heat, instead of light)*;
- Phonon-assisted Auger conversion processes.

Luminescent thermometers based on the intensity of a single transition are highly dependent of eventual illumination oscillations, signal-to-noise detection, absorption and scatter cross-sections,
and local fluctuations on the phosphor concentration. As recursive calibration procedures are not compatible with end-user applications a ratio of intensities must be employed.\cite{10,18}

### 4.1.1. Intensity ratio (FIR) or bandshape

The bandshape-based nanothermometry exploits the relative change in the intensity ratio of two independent energy-close transitions. Both emission lines can be generated from a single luminescent center (single-center thermometers) or they can result from two distinct emitting centers (dual-center thermometers).\cite{16,17} The use of single-center thermometers was introduced by Kusama et al.\cite{92} in a seminal paper (Collins et al.\cite{147} and Wade et al.\cite{148} give a review of the technique).

In single-center ratiometric thermometers, \( \Delta \) (or FIR) is defined using the emission intensities of the \(|2>\rightarrow|0>\) \((I_{02} \equiv I_2)\) and \(|1>\rightarrow|0>\) \((I_{01} \equiv I_1)\) transitions, where \(|0>\) denotes the ground level and \(|1>\) and \(|2>\) the two thermally-coupled excited levels (level \(|2>\) is more energetic than level \(|1>\)):\cite{148-150}

\[
\Delta = \frac{I_2}{I_1} = \frac{A_{02} \hbar \nu_{02} N_2}{A_{01} \hbar \nu_{01} N_1} \quad (9)
\]

where \(N_1\) and \(N_2\) are the populations of the \(|1>\) and \(|2>\) levels, \(\nu_{01}\) and \(\nu_{02}\) are the frequencies of the \(|1>\rightarrow|0>\) and \(|2>\rightarrow|0>\) transitions, and \(A_{01}\) and \(A_{02}\) are the total spontaneous emission rates from levels \(|1>\) and \(|2>\) to level \(|0>\). Note that Eq. 9 assumes that the intensities \(I_2\) and \(I_1\) are corrected by the instrument response and, as mentioned above, should also consider the Jacobian transformation. Furthermore, if the depopulation of the \(|1>\) and \(|2>\) energy levels involves other energy levels beyond \(|0>\), Eq. 9 must be corrected by the \(\beta_2/\beta_1\) ratio, where \(\beta_i\) \((i=1,2)\) are the branching ratios of the \(|i>\) level \((i.e.,\, the\, percentage\, of\, the\, total\, emission\, from\, the\, thermalized\, level\, (|1>\, or\, |2>)\, to\, the\, final\, |0>\, state)\). If the two high-energetic levels are in thermal equilibrium (they are called by “thermally-coupled levels”, with energetic separations of the order of the thermal energy \(k_B T\)), \(N_1\) and \(N_2\) are related by:

\[
N_2 = \frac{g_2}{g_1} N_1 \exp \left(-\frac{\delta E}{k_B T}\right) \quad (10)
\]
where \( g_1 \) and \( g_2 \) are the degeneracies of the two levels and \( \delta E \) is the energy gap between the barycenters of the \(|1>\rightarrow|0>\) and \(|2>\rightarrow|0>\) emission bands. Eq. 9 is, thus, written as:

\[
\Delta = \frac{g_2 A_{02} \hbar \nu_{02}}{g_1 A_{01} \hbar \nu_{01}} \exp \left( -\frac{\delta E}{k_B T} \right) = B \exp \left( -\frac{\delta E}{k_B T} \right),
\]

with \( B = \frac{g_2 A_{02} \nu_{02}}{g_1 A_{01} \nu_{01}} \). The two emitting levels cannot be too separated in energy, otherwise its thermalization is not detected. Typically, they are considered “thermally-coupled” (e.g., in a thermodynamically quasi equilibrium state) for \( \delta E \) ranging from 200 to 2000 cm\(^{-1}\).[151]

Up to know, in most of the examples involving the temperature determination in single-center thermometers based on the FIR of “thermally-coupled” levels, the \( \delta E \) and \( B \) parameters result from a fit (e.g. are not determined independent of the temperature), and, therefore, an external thermal calibration of the thermometric parameter is required. The typical calibration process needs an independent temperature measurement, using a thermocouple, a pyrometer or an infrared thermal camera, for instance, to permit the intensity-to-temperature conversion. As follows, a new calibration procedure is mandatory whenever the thermometer works in an alternate medium or a different environment, with altered ionic strength, pH, pressure, ions local neighborhoods, or atmosphere composition, that disturb the thermometric parameter and, thus, the calibration. Moreover, recording several calibration curves in various medium is a tedious task that is not always possible, as mentioned previously, and, generally, a single calibration relation is assumed to be valid, independent of the medium. This \textit{ad hoc} assumption is a fundamental bottleneck of secondary luminescent thermometers.

However, recently Balabhadra \textit{et al.}\[140\] realized that \( \delta E \) and \( B \) can be measured independently of any experimental calibration procedure, demonstrating that single-center thermometers based on two thermally-coupled electronic levels are intrinsically luminescent primary thermometers. This was a significant step forward because it means that any thermometer based on Eq. 11 is, intrinsically, a primary thermometer, and, therefore, the equation can be used to predict the temperature calibration curve independently of the medium.[10, 140, 152] The \( \delta E \) value is determined using the formal definition of barycenter of a \( J-J' \) transition (\( J \) stands for the total angular momentum) or, when experimental difficulties in assigning precisely the Stark-Stark transitions
exist, by an envelope fitting to the $I_1$ and $I_2$ transitions,[61] see Figure 7a for the example of the $^2\text{H}_{11/2} \rightarrow ^4\text{I}_{15/2}$ and $^4\text{S}_{3/2} \rightarrow ^4\text{I}_{15/2}$ Er$^{3+}$ transitions. The parameter $B$ is empirically inferred from the plot of $\Delta$ versus laser excitation power, Figure 7b.[10, 140] When the laser-induced heating is negligible, (i.e. in the limit of null excitation power), the temperature, $T_0$, corresponds the room-temperature[153, 154] and the thermometric parameter $\Delta_0$ is given by:

$$\Delta_0 = B \exp\left(-\frac{\delta E}{k_B T_0}\right).$$

(12)

The absolute temperature value is determined by the ratio $\Delta/\Delta_0$ (calculated as the ratio between Eq. 11 and Eq. 12) resulting:

$$\frac{1}{T} = \frac{1}{T_0} - \frac{k_B}{\delta E} \ln\left(\frac{\Delta}{\Delta_0}\right).$$

(13)

This approach was validated for the seminal example of the $^2\text{H}_{11/2} \rightarrow ^4\text{I}_{15/2}$ ($I_H=I_2$) and $^4\text{S}_{3/2} \rightarrow ^4\text{I}_{15/2}$ ($I_S=I_1$) Er$^{3+}$ transitions ($^2\text{H}_{11/2}$ and $^4\text{S}_{3/2}$ are thermally-coupled energy levels[147, 149]), using as an illustrative example SrF$_2$:Yb$^{3+}$/Er$^{3+}$ UCNPs (Yb$^{3+}$/Er$^{3+}$ is by far the widely reported pair in Ln$^{3+}$-luminescent thermometry).[140] The temperature calculated through Eq. 13 was compared with the readout of conventional thermometers positioned in contact with the particles (for powders) or immersed in aqueous suspensions (Figure 7c). A remarkable agreement between the predicted and measured temperature values is observed, irrespectively of the NP’s size and of the dispersion media, demonstrating that for this example no other variables apart temperature impact the thermometric parameter value. We should note that this approach is general and is extensible to any other thermometer based on two “thermally-coupled” levels, albeit up to now was solely applied to the $^2\text{H}_{11/2}$ and $^4\text{S}_{3/2}$ emitting levels.

The parameter $B$ can be also calculated using the Judd–Ofelt theory.[155, 156] For that, let us consider the integrated coefficient of spontaneous emission of a transition between $J$ and $J'$ manifolds as:[42, 157, 158]
where \( e \) is the electronic charge, and \( n \) is the refractive index of the medium. The electric (\( S_{ed} \)) and magnetic (\( S_{md} \)) dipole strengths are given (in units of \( e^2 \)) by:

\[
S_{ed} = \frac{1}{(2j + 1)} \sum_{\lambda=2,4,6} \Omega_{\lambda} \left| \langle J' || U^{(\lambda)} || J \rangle \right|^2
\]

\[
S_{md} = \frac{\hbar^2}{16\pi^2mc^2} \left| \langle 0 || L + 2S || i \rangle \right|^2
\]

where the quantities \( \Omega_{\lambda} \) (\( \lambda = 2, 4, 6 \)) are the so-called Judd–Ofelt intensity parameters\(^{155, 156} \) and \( m \) is the electron mass. The \( \langle ||U^{(\lambda)}|| \rangle \) and \( \langle ||L+2S|| \rangle \) are reduced matrix elements (tabulated by Carnal et al.\(^{159} \)) and the angular operators \( L \) and \( S \) are in units of \( \hbar \). The \( \Omega_{2,4,6} \) parameters in Eq. 15 are phenomenologically obtained from the absorption\(^{160} \) or, in the special case of the Eu\(^{3+} \) ion,\(^{42} \) also from the emission spectra, permitting the calculus of the coefficients of spontaneous emission and \( B \) parameter. For the \( ^2H_{11/2} \rightarrow ^4I_{15/2} \) (\( \nu_H \equiv \nu_2 \)) and \( ^4S_{3/2} \rightarrow ^4I_{15/2} \) (\( \nu_S \equiv \nu_1 \)) induced electric-dipole transitions \( B \) is given by:\(^{150, 161, 162} \)

\[
B = \frac{\nu_2^4 \beta_2}{\nu_1^4 \beta_1} \frac{\sum_{\lambda=2,4,6} \Omega_{\lambda} \left( \left| \langle ^2I_{11/2} || U^{(\lambda)} || ^4H_{11/2} \rangle \right|^2 \right)}{\Omega_6 \left( \left| \langle ^2I_{11/2} || U^{(6)} || ^4S_{3/2} \rangle \right|^2 \right)}
\]

\[
\approx \frac{\nu_2^4 \beta_2}{\nu_1^4 \beta_1} \frac{0.7158 \Omega_2 + 0.4138 \Omega_4 + 0.0927 \Omega_6}{0.2225 \Omega_6}. \tag{17}
\]

Surprisingly, and as far as we know, this calculation has been scarcely reported. Examples include the \( I_H \) and \( I_S \) transitions in Er\(^{3+} \)-based oxyfluoride glass/glass-ceramic\(^{150} \) and La\(_2\)S\(_3\):Yb\(^{3+}/\)Er\(^{3+} \),\(^{162} \) and the \( ^4F_{3/2} \rightarrow ^4I_{9/2} \) and \( ^4F_{5/2} \rightarrow ^4I_{9/2} \) lines in SrF\(_2\):Nd\(^{3+}\)\(^{163} \) crystalline powders.
4.1.2. Bandwidth

Generally, the emission lines of phosphors broaden as temperature increases. This is ascribed to the intrinsic vibrations of the lattice (homogeneous broadening, highly temperature dependent), or to the presence of different optical centers and defects (inhomogeneous broadening, slightly temperature dependent). Henderson and Imbusch described the temperature dependence of the bandwidth \( W \) of emission and absorption bands as:\[^{164}\]

\[
W(T) = W_0 \sqrt{\coth\left(\frac{h\Omega}{2k_BT}\right)}
\]  

(18)

where \( W_0 \) is the full width at half maximum (FWHM) of the band at 0 K, and \( h\Omega \) is the phonon energy (lattice vibration) that interacts with the electronic transitions.

There are few reports using intra 4f line’s emission bandwidth to measure the temperature, despite all of them present the functional form predicted by Eq. 18. Strangely, none of these reports used Eq. 18 to extract the energy of the phonon responsible for the broadening. Peng et al., for instance, used the \( ^5D_0 \rightarrow ^7F_2 \) transition in the \( \text{Y}_2\text{O}_3:\text{Eu}^{3+} \) phosphor to determine the temperature in the 10–670 K range.\[^{165}\] The transition bandwidth remains essentially unaltered for \( T<70 \) K, broadening linearly for higher temperatures at a rate of 0.078 cm\(^{-1}\)·K\(^{-1}\), corresponding to \( S_m=0.78 \) %·K\(^{-1}\) (at 70 K).\[^{165}\] In another example, Wang et al. analyzed the bandwidth of several \( \text{Tm}^{3+} \) emission lines in \( \text{NaYbF}_4:\text{Tm}^{3+}@\text{SiO}_2 \) core@shell microparticles (Figure 8).\[^{166}\] Among the transitions studied, the \( 1^D_2 \rightarrow 3^F_4 \) (350 nm) and \( 3^H_4 \rightarrow 3^H_6 \) (798 nm) ones broaden linearly with increasing temperature (100-700 K).\[^{166}\] Using a \( \text{YAlO}_3:\text{Nd}^{3+} \) nanoperovskite, Hernández-Rodríguez et al.\[^{167}\] compared the thermometric performance of the material using the FIR method (\( ^2\text{H}_{9/2},^4\text{F}_{5/2} \rightarrow ^4\text{I}_{9/2}/^4\text{F}_{3/2} \rightarrow ^4\text{I}_{9/2} \)) and the FWHM of a Stark component of the \( ^4\text{F}_{3/2} \rightarrow ^4\text{I}_{13/2} \) transition. The corresponding \( S_m \) values are 1.8%·K\(^{-1}\) and 3.3%·K\(^{-1}\), for the FIR method and the FWHM change, respectively (at 293 and 370 K, respectively). The corresponding temperature uncertainty values are 0.9 and 0.4 K. Although this example points out the benefit of using the spectral bandwidth approach for temperature determination, more studies are required to infer if this conclusion can be generalized for other systems.
Tm$^{3+}$-doped crystalline TiO$_2$ films$^{[168]}$ and the [Eu(keto)$_3$(H$_2$O)]$^{[169]}$ (keto=ketoprofen) coordination compound are interesting and atypical examples of Ln$^{3+}$-based luminescent thermometers reporting simultaneously temperature-induced bandwidth increase and wavelength shift. In the former example, the $^3F_{3,0} \rightarrow ^3H_{6,0}$ Tm$^{3+}$ transition (at 676 nm) exhibits a linear wavelength blue-shift $\frac{d\lambda}{dT}$ of $-2.2 \text{ pm} \cdot \text{K}^{-1}$ $(+0.048 \text{ cm}^{-1} \cdot \text{K}^{-1})$ with a 1.25 nm $(55 \text{ cm}^{-1})$ bandwidth increase, over the $\sim$85–750 K range. This linear behavior is in contrast with that exhibited by the conventional Al$_2$O$_3$:Cr$^{3+}$ optically-based thermometers in which the peak-shift linear behavior only covers a limited region $(\sim$300–600 K), being the bandwidth and temperature precision highly affected at increasing temperatures.$^{[168]}$ For [Eu(keto)$_3$(H$_2$O)], whereas the FWHM of the $^5D_0 \rightarrow ^7F_0$ Eu$^{3+}$ transition shows small variations $(\leq 3.0 \text{ cm}^{-1}$, the experimental resolution), its energy displays a linear blue-shift as temperature increases from 25 to 300 K, the maximum splitting is $16.6\pm3.0 \text{ cm}^{-1}$.$^{[169]}$ In both examples, the electron–phonon coupling seems to plays a relevant role in the mechanism beyond the temperature dependence of the Ln$^{3+}$ transitions.

4.2. Time-resolved scheme: Lifetime

Unlike the luminescence intensity methods, the lifetime-based technique holds crucial advantage of virtually not being affected by the size, geometry and the concentration of the luminescent probe. Moreover, the value of lifetime shown to be independent on the effects of light scattering, reflection, and intensity fluctuations of the excitation source. However, lifetime determination needs a pulsed excitation source with long illumination and acquisition time which in turn leads to time-consuming measurements limiting the use of this technique. Nevertheless, and although the thermal readout of large temperature gradients at time intervals shorter than or equal to the lifetime of the luminescence is impracticable using this technique, the recent technological advances made simpler and less expensive the employment of the technique.

4.3. Comparing the time-integrated and time-resolved schemes

Albeit interesting, the comparison between the performance of the time-integrated and time-resolved temperature methods has not been done systematically. The pioneer work of Collins et al.$^{[147]}$ in Cr$^{3+}$-, Er$^{3+}$-, and Pr$^{3+}$-based crystals was one of the first examples doing it. The FIR response provides higher $S_t$ values (e.g., 5 times larger for the Pr$^{3+}$-based crystal). As lifetime
values are essentially temperature-independent in cryogenic temperatures range this is quite evident. The same conclusion was also inferred by Rai & Rai in Pr$^{3+}$-doped lithium tellurite glass,[170] Paviolo et al.[29] in fluorescent molecular thermometers based on rhodamine B (Rhb) and by Gálico et al.[171] in the [Eu(bzac)$_3$(H$_2$O)$_2$] complex (where bzac$^-$ stands for tris(1-phenyl-1,3-butanedione). Paviolo et al. realized that the temperature in an organic tissue’s cytoplasm measured via RhB emission intensity is more precise and reliable than that measured using the RhB lifetime,[29] while Gálico et al. reported $S_m=5.25\%\cdot K^{-1}$ (at 303 K) and $S_m=1.35\%\cdot K^{-1}$ (at 293 K)[171] through the temperature dependence of the integrated intensity of the $^5D_0 \rightarrow ^7F_2$ transition and the $^5D_0$ lifetime, respectively. Recently, Gharouel et al.[172] performed a systematic comparison of the performance of distinct Pr$^{3+}$-based thermometers operating over 298–363 K using either the thermal dependence of the ratio of two 4f transitions or of the decay time of an excited state. Similar $S_r$ values ranging from 0.25 to 0.60 $\%\cdot K^{-1}$ were obtained and, again, although the lifetime approach requires more complex detection systems, the thermal sensitivity outcome is, at best, the same that the one obtained by the FIR method.[172] Therefore, in general, the wisest approach should involves a ratiometric intensity response to temperature variations.

5. Luminescent thermometers based on Ln$^{3+}$ ions

5.1. Molecular complexes and organic-inorganic hybrids

Ln$^{3+}$-doped molecular systems (essentially with Eu$^{3+}$ and Tb$^{3+}$ ions) have been widely explored in luminescent thermometry, since the pioneering work of Sato et al. in 1989.[173] For a review on molecular Ln$^{3+}$-based thermometers see the work of Uchiyama et al.[14] More recent noteworthy and illustrative examples are the works of Susuki et al.,[174] Hatanaka et al.,[175] and Khudoleeva et al.[176] The first example showed real-time thermogenesis in a single HeLa cell using the Eu(tta)$_3$ complex (tt$a^-$ stands for 3-thenoyltrifluoroacetonate) dissolved in dimethyl sulfoxide. Temperature variations as small as 1 K in the physiological range were detected.[174] The second example used [Tb$_{0.99}$Eu$_{0.01}$ (hfa)$_3$(linker)$_n$]$_n$ polymers (where hfa$^-$ stands for hexafluoro acetylacetonate and four phosphine oxides were used as linkers) – so-called chameleon emitters, because the emission color gradually changes with the temperature – to demonstrate how the thermal sensitivity is controlled by the linker, as well as by the hfa ligand.[175] In the last example, surface modified tph@Tb$_{0.999}$Eu$_{0.001}$F$_3$ fluoride (tph$^-$=terephthalate) demonstrated non-toxicity
and cellular permeability, exhibiting *in vitro* Eu\(^{3+}\) and Tb\(^{3+}\) luminescence with \(S_t=0.35\%\) K\(^{-1}\) at 313 K.

The chemical and optical instability of the isolated molecular systems with the increasein of temperature,\(^{[177]}\) however, preclude effective thermometry applications and composite materials formed by polymers or organic-inorganic hybrid hosts incorporating the lanthanoid complexes rapidly became an attractive alternative. An illustrative and pioneering example is the thermal imaging of a metal stripe covered with a thin film of poly(methyl methacrylate) (PMMA) doped with the Eu(tta)\(_3\) complex.\(^{[95]}\) Despite the low temperature uncertainty (\(\delta T=0.08\) K) and the quite interesting spatial resolution (\(\delta x=0.7\) µm), the system is not ratiometric.

Using organic-inorganic hybrid materials as hosts, Brites *et al.*\(^{[15]}\) proposed groundbreaking thermometers based on the Tb\(^{3+}\) (\(^5\)D\(_4\)→\(^7\)F\(_5\)) and Eu\(^{3+}\) (\(^5\)D\(_0\)→\(^7\)F\(_2\)) emissions, at 545 and 612 nm, respectively. The key point on this approach is the rational design of the host permitting the occurrence of thermally-driven \(^5\)D\(_4\)→host energy transfer, keeping the population of the \(^5\)D\(_0\) emitting level unaffected. Then, the ratio between the intensity of the \(^5\)D\(_4\)→\(^7\)F\(_5\) and \(^5\)D\(_0\)→\(^7\)F\(_2\) transitions, \(I(^5\)D\(_4\)→\(^7\)F\(_5\))/I(^5\)D\(_0\)→\(^7\)F\(_2\)), gives the absolute temperature, with a spatial resolution determined by the size of the clusters to which the Ln\(^{3+}\) complexes are attached.\(^{[15]}\) We should note that this mechanism is dissimilar than that frequently reported in Tb\(^{3+}\)/Eu\(^{3+}\)-doped examples in which the temperature dependence of the \(I(^5\)D\(_4\)→\(^7\)F\(_5\))/I(^5\)D\(_0\)→\(^7\)F\(_2\)) ratio is controlled by Tb\(^{3+}\)-to-Eu\(^{3+}\) energy transfer mechanisms.\(^{[178]}\) The use of Tb\(^{3+}\)-to-Eu\(^{3+}\) energy transfer as a tool to temperature determination was firstly proposed by Sato *et al.* in 1989\(^{[173]}\) and later revisited by Liu *et al.* in 2005.\(^{[179]}\) Nevertheless, and undoubtedly inspired by the works of Sato *et al.*\(^{[173]}\) and Brites *et al.*,\(^{[15]}\) the \(I(^5\)D\(_4\)→\(^7\)F\(_5\))/I(^5\)D\(_0\)→\(^7\)F\(_2\)) ratio is currently, by far, the widely used thermometric parameter allowing in the 298–333 K range typical values of \(S_m=7.1\pm0.2\%\cdot\text{K}^{-1}\), \(\delta T=0.09\pm0.01\) K, \(R>99.2\%\),\(^{[131]}\) \(\delta x>0.5\) µm, and \(\delta t>0.005\) s (Table 1).\(^{[118]}\) For a review on luminescent thermometers based on organic–inorganic hybrids see Ref. \(^{[77]}\).

Recent examples on Tb\(^{3+}\)/Eu\(^{3+}\)-doped systems not discussed in this review and deserving remark are the works of Piñol *et al.*,\(^{[128]}\) Brites *et al.*,\(^{[131]}\) Rodriges *et al.*,\(^{[180]}\) and Ramalho *et al.* (Table 1).\(^{[181]}\) The first two examples are discussed in more detail in section 6.2. Rodriges *et al.*,\(^{[180]}\) reported the thermometric functionalization of a Si surface with Tb\(^{3+}\) and Eu\(^{3+}\) complexes leading to \(S_m=1.45\%\cdot\text{K}^{-1}\), \(\delta T=0.3\) K and cycle-recycle reliability of 98.6 %. The hysteresis of the luminescence of the material results in a dual-sensitive temperature regime. The observed
reversible bistability permits the Si-functionalized surface to operate as an optically active two-module molecular demultiplexer logic circuit, opening the possibility of use this computing molecule in medical- and biotechnologies, such as blood diagnostics, “lab-on-a-molecule” systems, and molecular computational identification of small objects. On the other hand, Ramalho et al.\textsuperscript{[181]} used a PMMA substrate coated with Tb\textsuperscript{3+}/Eu\textsuperscript{3+}-doped organic-inorganic hybrids to fabricate luminescent Quick Response (QR) codes.\textsuperscript{[181]} QR codes have gained increased attention as they offer a simple physical tool for quick access to web sites for advertising and social interaction. As QR codes are a widespread technology the adding of functionalities simultaneously with the increase of the storage capacity is a relevant technological issue. Luminescent QR codes based on transparent plastic substrates coated with Tb\textsuperscript{3+}/Eu\textsuperscript{3+}-doped organic-inorganic hybrids were reported, demonstrating the increase of storage capacity per unit area by a factor of two. A novel methodology to decode the multiplexed QR codes is developed based on a color separation threshold where a decision level is calculated through a maximum-likelihood criterion to minimize the error probability of the demultiplexed modules, maximizing the foreseen total storage capacity. The luminescent QR codes ability to sense temperature was demonstrated, as the Tb\textsuperscript{3+}/Eu\textsuperscript{3+}-based hybrids emission color coordinates varies with temperature (reproducibility higher than 93%), opening new fields of applications for QR codes as smart labels for sensing.\textsuperscript{[181]}

MOFs are a class of porous hybrid materials consisting of metal ions or clusters coordinated to organic ligand linkers.\textsuperscript{[182]} As the materials’ building blocks (metal ions, linkers and guest ions or molecules) are all potential sources of light emission, MOFs are appropriate platforms to engineering luminescence.\textsuperscript{[183-185]} Because the light-emitting centers of certain Ln\textsuperscript{3+}-bearing MOFs changes considerably with temperature, these materials have been explored in the last years as luminescent thermometers, especially based on the intensity ratio of two intra-4f transitions. The first reports on the subject by Cui et al.\textsuperscript{[183, 184]} and Cadiau et al.\textsuperscript{[51]} (first Ln\textsuperscript{3+}-bearing nanoMOF working as luminescent thermometer) used the intensity ratio of the Tb\textsuperscript{3+} (\(^{5}D_{4}\rightarrow^{7}F_{5}\)) and Eu\textsuperscript{3+} (\(^{5}D_{0}\rightarrow^{7}F_{2}\)) emissions, following up closely the ideas reported by us a couple of years before.\textsuperscript{[15]} Nonetheless the MOF characteristic limited thermal stability limits effective thermometry applications much above room-temperature, they are promising and can compete with other thermometer materials in the cryogenic (<100 K) and biological (298–323 K) temperature ranges. In fact, we should note that among Ln\textsuperscript{3+}-based materials, Ln\textsuperscript{3+}-containing MOFs present the highest relative thermal sensitivity values reported so far, both in the cryogenic, \(S_{m}=31 \text{ %} \cdot \text{K}^{-1}\) (at
4 K),\textsuperscript{186} and in the physiological, $S_m = 16 \text{~%} \cdot \text{K}^{-1}$ (at 300 K),\textsuperscript{187} ranges (Table 1). Cui et al.\textsuperscript{50} and Rocha et al.\textsuperscript{52} reviewed recently the main concepts and ideas assisting the design of MOF-based thermometers.

Recent examples on Tb\textsuperscript{3+}/Eu\textsuperscript{3+}-doped systems not discussed in these reviews and deserving remark are the works of Liu et al.\textsuperscript{188} and Li et al.\textsuperscript{189} The first paper reported an in situ reduction and crystallization route for preparing Eu\textsuperscript{2+}/Eu\textsuperscript{3+}-doped MOFs. The materials exhibit intrinsic- and sensitized-emissions of Eu\textsuperscript{2+} and Eu\textsuperscript{3+} ions, besides a long-lived luminescence from ligand-to-metal charge transfer. A ratiometric luminescent thermometer was demonstrated based on the linear relation between temperature and the intensity ratio of Eu\textsuperscript{3+} (at 618 nm) and Eu\textsuperscript{2+} (at 427 nm) emissions between 9 and 293 K.\textsuperscript{188} The second example described a MOF-based thermometer based on Eu\textsuperscript{3+}-to-ligand back energy transfer and operative over a wide temperature range, including the physiological (12-320 K), upon excitation with visible light (450 nm).\textsuperscript{189}

5.2. Upconversion (UC) and upconverting nanoparticles (UCNPs)

Upconversion (UC) emission is a nonlinear process developed by Bloembergen,\textsuperscript{190} Auzel,\textsuperscript{191} and Ovsyankin and Feofilov.\textsuperscript{192} The distinct mechanisms of UC emission were extensively reviewed in the last years\textsuperscript{193} and there are a great number of Ln\textsuperscript{3+}-based UCNPs that were proposed for luminescence nanothermometry. The UC emission can be distinguished as single-center and multi-center, depending on whether the UC signal is generated by a single type of Ln\textsuperscript{3+} ion or by a combination of different Ln\textsuperscript{3+} ions. Interestingly, and as far as we know, there is no examples reported in the literature of downconverting luminescent thermometers.

5.2.1. Single-center UC nanothermometers

The most common UC systems are based on Yb\textsuperscript{3+} as a sensitizer and Er\textsuperscript{3+}, Ho\textsuperscript{3+} or Tm\textsuperscript{3+} as activators. Yb\textsuperscript{3+} acts as an effective sensitizer owing a large absorption cross-section at 980 nm, a wavelength easily available due to its use in telecommunications technology. Furthermore, the Yb\textsuperscript{3+} excited state energy level matches well with the excited states of the Er\textsuperscript{3+}, Tm\textsuperscript{3+} and Ho\textsuperscript{3+} thus allowing an efficient resonant energy transfer.

As an activator, Er\textsuperscript{3+} is one of the widely used ion due to its strongly temperature-dependent intense green emission arising from the $^2\text{H}_{11/2} \rightarrow ^4\text{I}_{15/2}$ (515-525 nm) and $^4\text{S}_{3/2} \rightarrow ^4\text{I}_{15/2}$ (535-545 nm).\textsuperscript{147, 149} Based on that emission, Rodrigues et al. measured one of the highest $S_T$ values reported
so far for upconversion thermal sensing using $\beta$-NaGd$_{0.94}$Pr$_{0.02}$Er$_{0.02}$Yb$_{0.02}$F$_4@3$NaY$_{0.8}$Yb$_{0.2}$F$_4$ core@shell NPs.\textsuperscript{[194]} Under 980 nm irradiation, the visible Er$^{3+}$ emission shows a relative thermal sensitivity in the 83−323 K range, reaching $S_m=9.52\%K^{-1}$ (at 83 K, Table 1). The intensity of those Er$^{3+}$ transitions together with that of the Eu$^{3+}$ $^5D_0\rightarrow^7F_2$ (603-643 nm) line were used by Nigoghossian \textit{et al.}\textsuperscript{[195]} to develop an intriguing example of a dual-mode nanothermometer. NaGdF$_4$:Yb$^{3+}$/Er$^{3+}$ UCNPs were synthesized and coated with a silica shell to which a Eu$^{3+}$ complex with tta$^-$ was incorporated. Whereas the Er$^{3+}$ UC emission was excited at 980 nm, the DS Eu$^{3+}$ signal (not ratiometric) was excited at 352 nm through the tta ligands. Measurements were recorded near the physiological temperature range (293−323 K), revealing $S_m=2.48\%K^{-1}/\delta T=0.47$ K (980 nm) and $S_m=2.67\%K^{-1}/\delta T=0.06$ K (352 nm), at 303 K. Moreover, because the Eu$^{3+}$ luminescence decreases with the increasing of the UV-light exposure time, the Eu(tta)$_3$-based complex anchored in the silica shell was tested as a UV sensor.

One of the limitations of the great majority of the nanothermometers fabricate up to now (including Er$^{3+}$-doped UCNPs) is a limited operating temperature range (typically not above 400 K), which prevents use in high-temperature applications, such as, for example, thermal barrier coatings and chemical reactors. Illustrative examples widening the temperature range of luminescent thermometers up to ca. 900 K are the works of Geitenbeek \textit{et al.} in silica-coated NaYF$_4$:Yb$^{3+}$/Er$^{3+}$ NPs,\textsuperscript{[196]} Brites \textit{et al.} in Sr$_2$GeO$_4$:Pr$^{3+}$ crystalline powders,\textsuperscript{[197]} and Kolesnikov \textit{et al.} in YVO$_4$:Nd$^{3+}$NPs.\textsuperscript{[198]}

Tm$^{3+}$ and Ho$^{3+}$ are the other activator ions most used for temperature sensing.\textsuperscript{[199–201]} An illustrative example is Y$_2$O$_3$:Yb$^{3+}$/Ho$^{3+}$ submicrometric porous powders (using 978 nm excitation) reported by Lojpur \textit{et al.}\textsuperscript{[200]} presenting a maximum absolute sensitivity of 0.097 K$^{-1}$, at 85 K corresponding to $S_m=1.61\%\cdot K^{-1}$. Using the ratio between the intensity of the $^5F_4,^5S_2\rightarrow^5I_8$ transition and that of distinct Stark components of the $^5F_4,^5S_2\rightarrow^5I_7$ level in Ho$^{3+}$, yields to a maximum absolute sensitivity of 0.078 K$^{-1}$, that corresponds to $S_m=0.55\%\cdot K^{-1}$ (at 275 K).

When the intensity ratio is taken from two transitions arising from thermally-coupled levels, the thermometric parameter is given by Eq. 11 and accordingly to the definition of $S_r$, Eq. 2, results:

$$S_r = \frac{1}{B \exp\left(-\frac{\delta E}{k_B T}\right)} \times \left| \frac{\partial B}{\partial T} \exp\left(-\frac{\delta E}{k_B T}\right) - B \frac{\delta E}{k_B T^2} \exp\left(-\frac{\delta E}{k_B T}\right) \right| = \left| \frac{1}{B} \frac{\partial B}{\partial T} - \frac{\delta E}{k_B T^2} \right|. \quad (19)$$
If \( B \) is temperature independent, \( S_r \) only depends on \( \delta E \), decreasing monotonically with temperature increasing. On the contrary, if \( B \) is function of temperature, \( S_r \) also depends on the temperature dependence of the branching ratios of the two thermally-coupled levels, Eq. 17 (both the \( \Omega_{2,4,6} \) parameters and the frequencies of the two transitions involved in the thermometric parameter are temperature independent). This dependence on the branching ratios of the two thermally-coupled levels might justify eventual changes on the \( S_r \) values with system’s parameters, such as size, morphology, \( \text{Ln}^{3+} \) doping, or matrix’s phonon energy.

The impact of nanoparticle’s size on \( S_r \) values has been discussed in a few works.\(^{105, 202, 203}\) The first reference dates back to 2004 reporting a size dependence on \( S_r \) values for \( \text{BaTiO}_3: \text{Er}^{3+} \) nanocrystals in which the thermal parameter is the intensity ratio between the \( ^4S_{3/2} \rightarrow ^4I_{15/2} \) and \( ^2H_{11/2} \rightarrow ^4I_{15/2} \) \( \text{Er}^{3+} \) transitions.\(^ {105}\) As the size of the crystals decreases (from 60 to 26 nm) \( S_r \) increases, while the energy gap between the barycenters of the two transitions remains unchanged. Marciniak \textit{et al.}\(^{203, 204}\) also discussed a similar tendency in \( \text{NaYF}_4: \text{Yb}^{3+}/\text{Er}^{3+} \) and \( \text{LiLaP}_4\text{O}_{12}: \text{Yb}^{3+}/\text{Er}^{3+} \) nanophosphors. At 200 K, \( S_m \) raises from 1.1 \( \% \cdot \text{K}^{-1} \) to 2.1\( \% \cdot \text{K}^{-1} \), as the size of fluoride nanocrystals decreases from 200 to 8 nm, and from 1.1 \( \% \cdot \text{K}^{-1} \) to 1.8\( \% \cdot \text{K}^{-1} \), as the size of tetraphosphate nanocrystals decreases from 240 to 20 nm. An opposite trend, however, was reported by Dong \textit{et al.}\(^{202}\) on \( \text{NaYF}_4: \text{Yb}^{3+}/\text{Er}^{3+} \) microspheres (size from 0.7 to 2 \( \mu \text{m} \)) showing that \( S_a \) decreases as size increases, \( S_m=1.4 \% \cdot \text{K}^{-1} \) (700 nm) and \( S_m=1.0 \% \cdot \text{K}^{-1} \) (1600 nm) (at 223 K), as calculated by us. Intriguingly, both trends were attributed to the larger specific surface area of the smaller crystals. As the size of the crystal decreases, a relatively large number of optically active ions are located at the surface and its contribution becomes increasingly important, being influenced by nonraditive relaxation channels related to electron–phonon interactions that are stronger with increasing temperature.\(^{105, 202, 203}\) Moreover, the non-radiative rates of the two emitting levels might present a distinct temperature dependence and when the size of the nanoparticle decreases the material’s phonons density changes inducing a dependence of those rates with the crystal size. However, Balabahadra \textit{et al.}\(^{140}\) and Brandão-Silva \textit{et al.}\(^ {205}\) do not observe significant changes on \( S_r \) values with the decrease of the particle size in \( \text{SrF}_2: \text{Yb}^{3+}/\text{Er}^{3+} \) (size from 10 to 41 nm) and \( \text{Y}_2\text{O}_3: \text{Er}^{3+} \) (21 to 86 nm) NPs, respectively. Clearly, the influence of the nanoparticle’s size on the thermal sensitivity of luminescent thermometers seems to be dependent of the host and of the electron-phonon interactions requiring a deep and systematic analysis.
In summary, single-centered UC thermometers are essentially being reported based on the analysis of the emission intensity of two thermally-coupled energy levels. Although these systems are intrinsically primary thermometers (see section 2), the tight restriction in the energy gap $\delta E$ to ensure the strong coupling between the two levels, typically $\delta E < 2000 \text{ cm}^{-1}$,[83] implies $S_T$ values typically smaller than those characteristic of the downshifting examples (section 5.3 and Table 1). Larger energetic separation between the thermally-coupled levels decreases the thermalization of the upper energetic level, resulting in poorer luminescence intensity. To overcome this limitation, strategies for further $S_T$ enhancement other than thermally-coupled levels for designing FIR-based thermometers should be considered, besides playing with the size of the NPs or with the phonon energy of the hosts (as discussed above). A wisest approach consists in using two distinct (and thermally decoupled) emission lines of the same Ln$^{3+}$ emitting center, or to use two emitting levels of distinct Ln$^{3+}$ emitting centers, as discussed in the next section. The recent review by Cheng et al.[83] discusses strategies to improve $S_T$ values by using thermometric parameters based on “fully-decoupled” or “moderately-coupled” emitting levels or emitting levels in which the energy transfer is mediated or thermally-assisted by a host or a ligand level.

5.2.2. Multi-center UC nanothermometers

Multicenter UC thermometry exploits the different thermal dependence of the intensity of two lines generated in distinct Ln$^{3+}$ ions. The transitions can be fully thermally decoupled (e.g. both transitions decrease upon temperature raise) or can present an indirect thermal coupling (e.g. energy exchange mediated by the ion host or ligands). Both the possibilities have been reported extensively in the literature, being the energy transfer engineered via smart-chemical design of the thermal probe. The core@shell structure architecture allows a facile incorporation of dopants to guide an efficient energy transfer among different ions. Although multi-core@shell structures have been considerably reported for non-contact temperature measurements,[206, 207] there are only few works on multi-center UCNPs.[208-211]

An intriguing example was reported by Xu et al. using a Yb/Ho/Ce:NaGdF$_4$@Yb/Tm:NaYF$_4$ core@shell structure, presenting $S_m=2.4 \% \cdot K^{-1}$ (at 298 K) in the absence of Ce$^{3+}$. The thermometric parameter is defined using the red (Ho$^{3+}$: $^5F_5 \rightarrow ^5I_8$ and Tm$^{3+}$: $^4G_4 \rightarrow ^4F_4$ transitions) and the green (Ho$^{3+}$: $^5S_2$, $^5F_4 \rightarrow ^5I_8$ transition) bands. Introducing Ce$^{3+}$ in the core the authors can tune $S_m$ between 0.7 and 4.4 $\% \cdot K^{-1}$ via the efficient cross relaxation processes between Ce$^{3+}$ and Ho$^{3+}$(Figure 9).[210]
Recently Savchuk et al.\cite{132} reported KLuWO$_4$:Tm$^{3+}$/Ho$^{3+}$ NPs as tunable multifunctional heater-thermometer nanoplatforms under 808 nm excitation. The intensity ratio is defined using the intensity of the Tm$^{3+}$ $^3F_{2,3} \rightarrow ^3H_6$ line (at 696 nm) and that of Ho$^{3+}$ $^5S_2;^5F_4 \rightarrow ^5I_7$ (at 755 nm) one, with $S_m=2.8\%$ K$^{-1}$ and $\delta T=0.2$ K (at 300 K).

5.3. Downshifting (DS) and downshifting nanoparticles

Downshifting (DS) is a single photon process where upon excitation with a high-energy photon (typically in the UV region of the electromagnetic spectrum) a non-radiative relaxation occurs pursued by radiative relaxation, thereby resulting in the emission of a lower-energy photon. As an explanatory example we can mention the work of Ishiwada et al.\cite{212} that reported Tb$^{3+}$/Tm$^{3+}$:Y$_2$O$_3$ NPs as visual thermo-sensors, working in the 323–1123 K range. The intensity ratio between the Tm$^{3+}$ ($^1G_4 \rightarrow ^3H_6$) and the Tb$^{3+}$ ($^5D_4 \rightarrow ^7F_5$) lines is strongly temperature-dependent, under 355 nm (UV) excitation with $S_m=0.33\%\cdot$K$^{-1}$ (at 750 K). Lifetime based examples were also discussed, although in minor number, for the reasons addressed in section 4.3. The temperature dependence of the $^4S_{3/2}$ lifetime in the NaY$_2$F$_5$:Yb$^{3+}$/Er$^{3+}$ NPs\cite{56} presents $S_m=2.75\%\cdot$K$^{-1}$ (at 330 K), Figure 10. The authors tentatively attributed the shortening of the lifetime with the temperature increasing to non-radiative relaxation and multiphonon phenomena.

Several Ln$^{3+}$ pairs were used for DS nanothermometry, such as Tb$^{3+}$/Eu$^{3+}$,\cite{15,49,51,55} Nd$^{3+}$/Yb$^{3+}$,\cite{213} and Tm$^{3+}$/Ho$^{3+}$,\cite{211} However, most of the examples discussed in recent years are based on Nd$^{3+}$, driven by potential bioimaging applications.\cite{214} Nd$^{3+}$ is of particular interest because its ladder-like particular intra-4$f$ electronic configuration favors NIR excitation (around 800 nm) and emission within the first (650–950 nm), second (1000–1400 nm), and third (1550–1870 nm) biological transparency windows, where the living tissues present low optical absorption.\cite{215,216} Nd$^{3+}$ displays essentially five main transitions: $^4F_{5/2} \rightarrow ^4I_{9/2}$ (800–850 nm), $^4F_{3/2} \rightarrow ^4I_{9/2}$ (880–1000 nm), $^4F_{3/2} \rightarrow ^4I_{11/2}$ (1000–1210 nm), $^4F_{3/2} \rightarrow ^4I_{13/2}$ (1300–1480 nm) and $^4F_{3/2} \rightarrow ^4I_{15/2}$ (1700–1850 nm), matching efficiently the three biological windows.\cite{18,82,217} Most of the examples of thermometers based on DS are complex systems discussed in the following section.
5.4. Complex systems

In this section, we discuss illustrative examples of complex thermometric systems comprising multiple core@shell nanostructures,[207, 218-220] polymer- and hybrid-based materials,[30, 154, 221-224] and heater-thermometer nanoplatforms.[154, 225]

Multiple core@shell architectures are attracting much interest in recent years due to the possibility of combining distinct functions on a single nanostructure (see Ref.[220] for an updated review). An interesting approach is the use of these structures as double ratiometric nanothermometers. The first reported example used Yb⁺³/Er⁺³ co-doped NPs covered with a Yb⁺³/Nd⁺³ co-doped shell,[219] although more recently water dispersible nanoplatforms, with excitation and emission within the second and third biological optical transparency windows, were fabricated.[218] In the first example, temperature dependent Er⁺³ UC emission and Yb⁺³/Nd⁺³ DS emission were observed with \( S_m = 2.0 \%\cdot K^{-1} \) (at 200 K, Er⁺³-based core thermometer) and \( S_m = 2.5 \%\cdot K^{-1} \) (at 365 K, Yb⁺³/Nd⁺³-based shell thermometer).[219] The second case comprises a core (NaGdF₄) co-doped with Er⁺³/Ho⁺³/Yb⁺³ followed by i) a first shell of Yb⁺³; ii) a second shell co-doped with Yb⁺³/Nd⁺³, and iii) an additional passivation layer. The core@multishell structure was stabilized by a polyethylene glycol-grafted phospholipid and oleate. By using a heating-free 800 nm excitation, Ho⁺³/Nd⁺³ (1180–1340 nm) and Nd⁺³/Er⁺³ (1340–1550 nm) NIR emission band ratios were used for luminescence thermometry, both displaying similar relative thermal sensitivities (1.1% K⁻¹).[218]

Yang et al.[207] prepared by a multistep synthetic procedure a nanoplatform based on a Fe₃O₄ core coated by a middle SiO₂ shell and an NaYF₄:Nd⁺³ outer layer. The multi core@shell architecture showed excellent photostability, and impressive superparamagnetic properties (Figure 11). Under 806 nm continuous laser excitation the NPs exhibited three emission bands located within the NIR biological windows. The transparency of an ex-vivo tissue was tested presenting a clear larger penetration deep for \( \lambda < 1200 \text{ nm} \), Figure 11.[207] Wang et al.[226] constructed a complex NaLuF₄:Gd⁺³/Yb⁺³/Er⁺³@NaLuF₄@Yb⁺³@NaLuF₄:Nd⁺³/Yb⁺³@NaLuF₄ core@shell system able of emitting both UC and DC luminescence under 808 nm excitation (Figure 12). The intensity ratio using the Yb⁺³ 980 nm (²F₅/₂ → ²F₇/₂) and the Er⁺³ 1532 nm transitions (⁴I₁₃/₂ → ⁴I₅/₂) was used for in vivo NIR imaging studies. An Er⁺³-based UC nanothermometer using NaLuF₄:Yb⁺³/Er⁺³@NaLuF₄@Carbon core@shell@shell NPs with \( S_m = 1.0 \%\cdot K^{-1} \) and \( \delta T = 0.5 \text{ K} \) (at 308 K) was reported by Zhu et al.[67] The particles were internalized both in vitro and in vivo...
to obtain a temperature-feedback from real-time monitoring the microscopic temperature in photodynamic thermal therapy (Figure 13).

As mentioned previously, an important research line in Ln\(^{3+}\)-based luminescent thermometers explore the potential of polymers and organic-inorganic hybrids as host materials. The interesting example by Huang \textit{et al.}\cite{221} reported a hybrid nanocarrier consisting of Yb\(^{3+}/Er\(^{3+}\) co-doped NaGdF\(_4\) NPs encapsulated in the aqueous core of liposomes. The 980 nm excitation is used simultaneously to induce the Er\(^{3+}\) green UC emission and for drug delivery, by co-loading the doxorubicin (DOX) model anticancer drug with the UCNPs in the liposome nanocarrier. Additionally, a quenching on the green emission was ascribed to the donor UCNPs-to-acceptor DOX energy transfer, allowing the spectral monitoring of the DOX loading and release from the liposome nanocarriers.\cite{221} Although the authors do not report temperature determination the emission spectra of the nanoplatform can be also used with that purpose.

The combination of Ln\(^{3+}\)-based phosphors with other emitting centers was also exploited. Cerón \textit{et al.}\cite{54} developed a complex system joining in a hybrid nanostructure Nd\(^{3+}\)-doped NaGdF\(_4\) NPs, semiconductor PbS/CdS/ZnS QDs and poly(lactic-co-glycolic acid). The thermometric parameter is based on the strongly temperature-dependent emission at 1220 nm (arising from the QDs) and a temperature-independent reference peak at 1060 nm (the Nd\(^{3+}\)\(^4\)\(F_{3/2}\)\(\rightarrow^4\)\(I_{11/2}\) line). The coexistence of these two emissions allows to obtain \(S_m=2.5 \text{ %} \cdot \text{K}^{-1}\) (at 303 K, Table 1).

Heater-thermometer nanoplatforms are other interesting systems because they combine the heat release and temperature monitoring in a single nanostructure. One of the most exploited strategies consists in use plasmonic nanostructures and luminescent thermometers to achieve a fully non-contact control of the system. One of the first examples was reported by Debasu \textit{et al.}\cite{154} that developed a single nanoplatform integrating laser-induced heat generation by Au NPs and temperature sensing up to 2000 K via Gd\(_2\)O\(_3\):Yb\(^{3+}/Er\(^{3+}\) nanorods. The temperature determination is done based on the green Er\(^{3+}\) upconversion emission and Boltzmann’s law, for temperatures until 1200 K, and using the blackbody emission and the Planck’s law of blackbody radiation for temperatures until 2000 K.

Other illustrative example combines Au nanorods and NaGdF\(_4\):Yb\(^{3+}/Er\(^{3+}\) UCNPs.\cite{225} The longitudinal surface plasmon resonance of the nanorods is tuned to 980 nm, in resonance with the Yb\(^{3+}\) absorption wavelength, so luminescence thermometry and heating can be simultaneously excited. As an added benefit the authors observe a luminescence enhancement until 9-folds due to
the proximity of the Er$^{3+}$ ions with the plasmonic structures. The temperature is controlled by the 980 excitation power and measured \textit{in situ} by the Er$^{3+}$ thermally sensitive luminescence.\cite{225} In a step forward, the same group reported a nanocomposite consisting of NaGdF$_4$:Yb$^{3+}$/Er$^{3+}$ nanoparticle, mesoporous SiO$_2$, Au nanorods and a photosensitizer. Under 980 nm irradiation, plasmonic and UC NPs are simultaneously excited leading to a plasmonic enhancement of the UC luminescence and a simultaneous temperature increasing. Upon laser irradiation, and after loading a Zn phthalocyanine photosensitizer into the mesoporous SiO$_2$, the UC visible light subsequently activates the photosensitizer to release reactive oxygen species.\cite{227}

6. \textbf{Current trends in lanthanide-based luminescent thermometers}

As highlighted in the introduction, in the last couple of years the focal point of luminescence thermometry has progressively moved from the synthesis and general characterization of new thermographic phosphors towards the use of the technique as a tool in bioimaging, early tumor detection, and for unveil properties of the thermometers themselves or of their local surroundings. The present section covers meaningful examples demonstrating this shift. Moreover, the section also summarizes recent developments to boost the thermal sensitivity of luminescent thermometers.\cite{228}

6.1. \textbf{Luminescence thermometry using Ln$^{3+}$ ions as a biomedical tool}

Eu$^{3+}$-based thermometers were used to visualize the temperature-distribution within living organisms at microscopic scales. A polymer incorporating Eu-tris(dinaphthoylmethane)-bistrictroctylphosphine oxide as a temperature sensitive probe and rhodamine 800 (Rh800) to provide a reference emission band enabled the temperature monitoring and mapping with $S_m=3.6 \text{ %} \cdot \text{K}^{-1}$ and $1.4<\delta T<1.0 \text{ K}$. The polymer embedding the thermal probes successfully detected \textit{in vivo} temperature shifts at localized sites in the muscle of a living beetle, either due to an external heat source (980 nm laser heating) or due to the animal’s voluntary muscle-activation (pre-flight preparation, Figure 14a-c). The Eu$^{3+}$/Rh800 intensity ratio was recorded in 5 distinct positions of the muscle (Figure 14d,e) presenting a dynamics similar to that monitored by an IR thermal camera.\cite{124} Moreover, the same research group developed free-standing nanosheets embedding the same emitting centers with superior flexibility and transparency, compared with the previous report, enabling the attachment onto the uneven surfaced living tissues without any glue (Figure
and the densification of muscle fibers covered by the thermometric film. The film was used to measure temperature shifts in a beetle’s dorsal longitudinal muscle (Figure 15c,d) during the voluntary heat production, with $\Delta T = 3.75 \% \cdot K^{-1}$ at 302 K and $\Delta T$ up to 0.75 K. Endogenous heat production transfer between muscle fibers were studied using the thermal mapping recorded using the Eu$^{3+}$-Rh800 stacked nanosheets with a spatial resolution at least at the single muscle fiber level (impossible to achieved through IR thermal cameras), leading to further understand physiological activities in three stimulations: before, during and after the beetle’s pre-flight preparation (Figure 15e).[123]

The absorption coefficient and thermal diffusivity of tissues was calculated by Ximendes et al.[129] using Yb$^{3+}$/Nd$^{3+}$-based thermal probes. The authors follow the time-dependent temperature relaxation process to calculate the thermal diffusivity of living tissues by luminescence thermometry (0.13±0.04 mm$^2$·s$^{-1}$) in good agreement with that reported for breast tissue at 810 nm (0.142 mm$^2$·s$^{-1}$).[129]

Zhu et al. demonstrated a programmed combination of chemotherapy (CT) and photothermal therapy (PTT) combining in a single system, NaLuF$_4$:Yb$^{3+}$/Er@NaLuF$_4$@Yolk-Shell-SiO$_2$-PdPc@DPPC-DOX UCNPs, a photothermal agent (octabutoxyphthalocyanine palladium (II), abbreviated as PdPc), and a thermal responsive drug release unit (1,2-dipalmitoyl-sn-glycero-3-phosphocholine, abbreviated as DPPC), as the vehicle of the DOX chemodrug (Figure 16).[229] By controlling the nanostructure’ temperature (using a 730 nm laser), the CT-PTT sequence can be designed to achieve programmed combination cancer therapy. When the dosages of DOX and heat are kept at low level (2.5 µM and 0.150 W cm$^{-2}$, respectively), programmed combination therapy can achieve 39 folds improvement in therapeutic effect in vitro in comparison with conventional combination therapy that simultaneously initiates CT and PTT.[229]

IR-emitting core@shell Er-Yb@Yb-Tm LaF$_3$ UCNPs were reported for subcutaneous thermal probing operating in the second and third transparency biological windows of tissues with thermal sensitivity of 5%·K$^{-1}$. The acquisition of time-resolved 2D thermal images in a small animal model was reported taking advantage of the high thermal sensitivity and large optical penetration into tissues, scanning the subcutaneous temperature images in a minimally invasive way. Moreover in-vivo subcutaneous thermal videos opened the possibility to develop new diagnosis and control techniques with potential impact in existing biomedicine methods (Figure 17).[125]
Without using Ln$^{3+}$ ions, Santos et al.$^{[127]}$ use the temporal decay temperature profiles monitored by Ag$_2$S IR nanothermometers to early-tumor diagnosis. Changes in tissues are discerned through changes in their thermal dynamics measured by thermal transient thermometry. Experimental data obtained in a murine model of melanoma reveal evident differences between the thermal relaxation dynamics of tumoral and healthy tissues even at the early stages of the tumor development (e.g., up to 7 days before changes could be detected by optical inspection, Figure 18). The same group used NIR emitting PbS/CdS/ZnS QDs as deep tissue nanothermometers to discriminate between the ischemic and inflammatory phases (that occur after artery ligation), using exclusively thermal transient thermometry. The authors distinguish between the ischemic and the healthy tissues by distinct temporal decays of the NIR luminescence. Furthermore the QDs were used for time monitoring the revascularization of tissues after temporal restriction of blood supply.$^{[126]}

6.2. Quantifying the materials properties through luminescence thermometry

Piñol et al. developed magnetic and thermometric NPs composed of $\gamma$-Fe$_2$O$_3$ superparamagnetic NPs recovered with Eu$^{3+}$ and Tb$^{3+}$ complexes and further polymeric layers to render aqueous stability.$^{[128]}$ The thermometer presents a high relative thermal sensitivity (5.8% K$^{-1}$) and low temperature uncertainty (0.5 K), whereas the NP demonstrated a relatively small heat capacitance. Taking advantage of the physical contact between the thermometer and the nanoheaters, the existence of an unexpected temperature gradient between the nanoheaters and the surrounding media for $t > 10$ s and relatively low heat powers ($10^{-16}$ W per heater) generated by an alternated magnetic field was grasped. Moreover, previously unrevealed changes in the local temperature during the first few seconds of heating ($t < 10$ s) are observed opening intriguing possibilities to study heat flow at sub-micrometric scales.$^{[128]}

In a recent work, Baral et al.$^{[230]}$ measured the local temperature of lithographically fabricated Au nanostructures or drop-casted Au nanoparticles (40 nm) deposited on the top of AlGaN:Er$^{3+}$ films combining near-field scanning optical microscopy (SNOM) with Er$^{3+}$ luminescence thermometry (in downshifting). The thermal images present spatial resolution limited only by the SNOM cantilever tip aperture (200 nm) allowing to measure the effective local temperature of the nanostructures, with temperature uncertainty near 1K and temporal resolution of 130 ms (still out of the sub-micrometer, sub-millisecond region, not covered so far by any example). The steady-
state thermal profiles of distinct sized clusters made from the Au NPs (excited with a 532 nm CW laser) show that the maximum temperature change and temperature decay length into the surrounding medium increases linearly with cluster radius.

Using Yb$^{3+}$/Er$^{3+}$-doped NaYF$_4$ nanocrystals of distinct sizes suspended in aqueous and organic solvents, Brites et al.$^{[130]}$ measured the instantaneous Brownian velocity of the suspended nanocrystals. A heat flux in the nanofluid medium was externally induced through the Joule effect and real-time temperature monitoring by upconversion thermometry allowed to calculate the time instant associated to the onset of the change in the thermometric parameter induced by temperature variation. This critical time was measured irradiating the nanofluids (980 nm) at different positions along the predesigned path of the heat flux permitting to determine the instantaneous Brownian velocity of the nanocrystals for distinct volume fractions, solvents and nanoparticle sizes, Figure 19.$^{[130]}$ This technique ought to give a more deep comprehension of the factors governing thermal conductivity, convective heat and mass transport in nanofluids.

Guided by the same general purpose of evaluate the material’s properties trough luminescence thermometry, the thermal conductivity of mesoporous SiO$_2$ and TiO$_2$ nanofilms was calculated using the luminescent temperature readout of Eu$^{3+}$/Tb$^{3+}$-codoped organic-inorganic hybrid probes.$^{[131]}$ Using first a 980 nm laser beam to promote the plasmonic heating of the nanostructures, the temperature decay after turning the heating beam off was followed by luminescence thermometry to further calculate the thermal conductivity of the films. The authors demonstrated that the reported non-contact and non-destructive strategy is able to estimate the nanolayers’ thermal conductivity in accordance with the values reported for similar nanostructures using evasive electrical methods, Figure 20.$^{[131]}$

The thermal conductivity of an AlGaN:Er$^{3+}$ film was also recently evaluated using luminescence thermometry.$^{[231]}$ The authors positioned an Au micro disk over a AlGaN:Er$^{3+}$ film deposited on a silicon substrate. Upon continuous 532 nm laser irradiation (power density of 6×10$^9$ W·m$^{-2}$) the Au microdisks have a temperature increase of ~20 degrees. By temporal-modulating of the 532 nm laser intensity the authors induced a temperature increase followed by the relaxation to the room-temperature, which is monitored by the luminescence decay of the $^2$H$_{11/2}$→$^4$I$_{15/2}$ and the $^4$S$_{3/2}$→$^4$I$_{15/2}$ transitions. The temperature is calculated using the ratio of the intensity decay curves and thus the heat-transfer dynamics was mapped with spatial resolution bellow 100 nm in the microsecond range. This work is able to follow the cooling of a single Au micro disk and to
measure the rate of heat dissipation to the environment, directly calculating the absolute thermal conductivity of the AlGaN:Er$^{3+}$ film (1.7 W·m$^{-1}$·K$^{-1}$) in agreement with the literature values.$^{[231]}$

The thermal resistance of KLuWO$_4$:Tm$^{3+}$/Ho$^{3+}$ NPs was also recently estimated using a fully noncontact approach through upconversion thermometry.$^{[132]}$ The thermal resistance of powder NPs in contact with air was computed from the instantaneous temperature profiles and it was found to be of the same order of magnitude than the interfacial thermal resistance between Si and NiSi$_2$ in Si-based heterostructured nanowires.$^{[132]}$

6.3. Exploring new strategies to enhance the thermal sensitivity

It is well known that temperature increase causes, in general, a loss in the light emission intensity that is known as thermal quenching, that limits the application of luminescent materials at higher temperatures. The thermal quenching is attributed to non-radiative relaxation pathways that are thermally activated because the material’s atomic vibrations (phonons) are heightened with the temperature increase.

For NPs, however, there is a quenching channel, the so-called energy migration-induced surface quenching, that does not exist in their bulk counterparts. Recently, Cui et al.$^{[232]}$ demonstrated that the energy migration-induced surface quenching in Yb$^{3+}$-doped NPs can be suppressed by increasing temperature, resulting in an uncommon luminescence thermal enhancement. A mechanism based on the effect of thermal lattice expansion on Yb$^{3+}$-mediated energy migration is proposed to be beyond that unusual effect. Furthermore, since 2015 it was understood that the thermal effects on the light emission of organic-capped UCNPs is a size-dependent phenomenon. Systematic studies on the emission intensity of the particles upon distinct temperatures were performed by Li et al.$^{[233, 234]}$ and Shao et al.$^{[235, 236]}$ The authors showed that at higher temperatures (e.g. 300-500 K) whereas the emission intensity is enhanced for particles smaller than a critical size (e.g. 20–30 nm), it is quenched for bigger particles. This effect was used to control of NPs’ emission color via modulation of the irradiation laser power or directly varying the temperature (through complex heating systems).$^{[233, 234, 236]}$ Although several models were advanced to explain these intriguing thermal effects, a recent explanation purposed by Zhou et al.$^{[228]}$ is being discussed in the literature. The authors observed an approximately 2000-fold enhancement in blue emission for 9.7 nm Yb$^{3+}$/Tm$^{3+}$-codoped organic-capped UCNPs at 453 K, justifying their observations by a phonon-assisted energy transfer from sensitizers to activators, populating up the intermediate excited state.
of the UC process. The authors ascribed the phonon to existence of an oxygen moiety chelating Yb$^{3+}$ ions, [Yb···O], present in the NPs due to the chelation Yb$^{3+}$ ions at the nanoparticle’s surface by carboxylic groups (of the capping molecules). A physical mechanism to fully explain this surface mechanism remains, however, absent.$^{[237]}$

This new design principle opens the possibility to design novel size-dependent thermal probes that, using two emitting centers, can present higher performance in comparison to the existing ones. We notice that single-center thermometers based on Eq. 13 do not benefit from the thermal enhancement effect in $S_r$. The minimum $\delta T$ value, however, is generally reduced because the relative uncertainty $\delta A/\Delta$ will be lower for small particles at higher temperatures. Moreover, the primary nature of these thermometers can be used to determine the absolute temperature of the nanoparticle, despite the presence of thermal enhancement or quenching effects. We can foresee that multi-center UC nanothermometers will have its thermal sensitivity increased from the current $1–3\% \cdot K^{-1}$ to values one order of magnitude higher just by taking the ratio between thermally enhanced and thermally quenched emissions.

Martinez et al.$^{[152]}$ described an electrothermal device built by the assembly of nanocomposite transparent films combining a PMMA matrix and a percolating network of Ag nanowires$^{[238, 239]}$ covered by UCNPs of distinct sizes and compositions. The devices are excellent platforms to thermally fine-tune the particles’ emission intensity and the NPs’ local temperature and, thus, the emission color is easily controlled through the heat dissipation in the electrothermal device (by simply applying different DC voltages). This strategy provides a guide to fabricate innovative and versatile multichromatic upconversion nanostructures whose spectral emission is externally adjusted by electrothermal control. From thermometric point of view, the devices incorporating Er$^{3+}$-doped NPs are inherently primary thermometers and the particle’s local temperature can be accessed directly, using the intensity ratio of the green emission bands ($^2H_{11/2}\rightarrow^4I_{15/2}/^4S_{3/2}\rightarrow^4I_{15/2}$), Eq. 13. Devices composed of small and large Ln$^{3+}$-doped NPs containing distinct dopants allow to estimate the temperature using the primary thermometer based on the Er$^{3+}$ $I_{11}$ and $I_{8}$ bands. The calculated temperature values were used to calibrate the secondary thermometer defined using a mixture of thermally enhanced and thermally quenched emission lines resulting in a relative thermal sensitivity of about $6 \% \cdot K^{-1}$. $^{[152]}$
7. Summary and perspectives

The field of luminescence thermometry is growing intensively showing significant breakthroughs in sensing, imaging, diagnostics and therapy, among other areas. This interest has been mostly encouraged because many of the present technological demands in areas such as micro and nanoelectronics, photonics, nanomedicine, micro and nanofluidics have reached a point such that the use of traditional contact thermal probes (liquid-filled and bimetallic thermometers, thermocouples, pyrometers, and thermistors) are not capable to make reliable measurements when spatial resolution enters to the submicron range. This limitation of conventional thermometers for small systems have spurred the development of luminescent micro and nanothermometers, a research topic leaving its inflationary epoch accounting nowadays for more than 2.5 % of the total publications in luminescence materials. Moreover, and from an industrial point of view, this predicted miniaturization is expected to bring to the market new nanoscale thermal probes. Despite the recently developed luminescent nanothermometers are radically more sophisticated encompassing complex synthesis procedures, the fundamental problems and the applications that are being addressed are analogous to those reported in the field’s infancy: the understanding of heat transfer and energy transfer mechanisms, the optimization of temperature readout and the developing of efficient and cost-effective sensors for front-edge medical and engineering tools.

Among the distinct emitting centers used in luminescence thermometry, including proteins nucleic acids, and other biomolecules, thermosresponsive polymers, organic dyes and QDs, many Ln$^{3+}$-based luminescent thermometers have been reported, essentially in the last decade. Systems comprise molecular complexes, MOFs, polymers and organic-inorganic hybrids, multifunctional heater-thermometer nanoplatforms, and UC, DC, and DS NPs. This review describes the use of these Ln$^{3+}$-based phosphors as luminescent ratiometric thermometers in diverse applications, with focus on what the authors believe that will be the emergent new research areas in this fascinating research field: the use of luminescence thermometry for thermal imaging, early tumor detection and as a tool for unveil properties of the thermometers themselves or of their local surroundings.

Finally, to become a consolidated subject and not a temporary fashion, the research on luminescent thermometry must settle down as a strong node of fertile interactions among disparate communities, such as chemists, physicists, engineers, theoreticians, biologists, and physicians. The cross-fertilization of ideas and experiences at these interfaces will certainly induce important and exciting breakthroughs in future years.
Acknowledgements

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**Figures and Tables**

![Figure 1](image)

**Figure 1.** Revenue generation for the global temperature sensors market (Grand View Research Inc.). Adapted from reference [12].
Figure 2. (a) Device for calibrating temperature-sensitive ZnCdS phosphors. The front view of the device displays the thermometers used for calibration, temperature increases from right to the left. The top image shows the phosphor upon UV excitation, with the brighter region corresponding to the lowest temperature. (b) Arrangement for studying air stream impinging upon phosphor screen. (c) High-contrast illustrative print of thermal pattern produced by the air stream. (d) Isotherms on the screen obtained from the set of prints like that presented in (c). Numbers are temperatures in degrees centigrade. Adapted from reference [88]. Copyright (1949), OSA Publishing.
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Table 1. Thermometric performance of illustrative examples of the distinct classes of Ln$^{3+}$-based luminescent thermometers discussed in this review, MOFs, NPs, complexes (C), core@shell systems (CS), UCNPs, and microparticles (P). The operating temperature ($\Delta T$) and spectral ranges ($\Delta \lambda$), as well as the optical parameter used in each example are also listed. Within each spectral range the examples are ordered by ascending $T_m$ values.

<table>
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<tr>
<th>$\Delta \lambda$</th>
<th>Material</th>
<th>$\Delta T$ (K)</th>
<th>$S_m$ (%·K$^{-1}$)</th>
<th>$T_m$ (K)</th>
<th>$\delta T$ (K)</th>
<th>Optical parameter</th>
<th>Ref.</th>
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<td>Y$_2$O$_3$:Nd$^{3+}$</td>
<td>NPs</td>
<td></td>
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</tr>
<tr>
<td>LaF$_3$:Er$^{3+}$/Yb$^{3+}$ @ LaF$_3$:Yb$^{3+}$/Tm$^{3+}$ (*)</td>
<td>UCNPs</td>
<td></td>
<td></td>
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</tr>
</tbody>
</table>

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acac: acetylacetonate; btfa: 4,4,4-trifluoro-1-phenyl-1,3-butane dicarboxionate; BW-I, BW-II, and BW-III: biological transparency window I (700-950 nm), II (1000-1350 nm) and III (1550-1870 nm); H$_2$cpda: 5-(4-carboxyphenyl)-2,6-pyridinedicarboxylic acid; CPDK: cyclopentene-1,4-dione; DPA: di-(2-pyridyl)amide; eddpo: ethylenediamine-N,N'-di(methylene phosphinic) acid; H$_2$FDC: 9-fluorenone-2,7-dicarboxylic acid; HL: 5-hydroxy-1,2,4-benzotriazinetricarboxylic acid; PDMS: polydimethylsiloxane; phen: phenanthroline; pyphen: pyrazino[2,3-f][1,10]phenanthroline; tfac: 1,1,1-trifluoro-2,4-pentanedionate; VIS: visible.

(*) Ratiometric parameter involving the ratio between the intensities of the Yb$^{3+}$ $^2$F$_{5/2}$$\rightarrow$$^2$F$_{7/2}$ (at 1000 nm, BW-II) and the Er$^{3+}$ $^4$I$_{15/2}$$\rightarrow$$^4$I$_{13/2}$ (at 1550 nm, BW-III) transitions.
Biographies & Table of Contents

Dr. Carlos D.S. Brites is a researcher in CICECO- Aveiro Institute of Materials of University of Aveiro. He obtained his Ph.D. in 2012 from the Department of Physics, University of Aveiro, and was a post-doc in the same department. His current research interests include the use of trivalent lanthanide ions as nanoscale luminescent probes for quantifying material’s properties.

Dr. Sangeetha Balabhadra is a Postdoctoral fellow in the School of Physical and Chemical Sciences, in University of Canterbury (New Zealand). She obtained her Ph.D. in Physics in 2017 from Department of Physics and CICECO-Aveiro Institute of Materials (Portugal). Her current research interests include synthesis and spectroscopy studies of lanthanide doped nanoparticles.

Prof. Luís D. Carlos is Full Professor in the Department of Physics at the University of Aveiro and vice-director of the CICECO-Aveiro Institute of Materials (Portugal). He is member of the Lisbon Academy of Sciences and of the Brazilian Academy of Sciences. His current research interests include luminescent nanothermometers, luminescent solar concentrators, organic-inorganic hybrids for green photonics (solid-state lighting and integrated optics), and single-ion and single-molecule magnets.
The field of luminescent thermometers based on lanthanide-bearing materials is reviewed, from the first developments of the field in the 1950-1960’s until the most recent cutting-edge examples. The main concepts, ideas and grand challenges are discussed, including the current movement towards the use of luminescent thermometry as a tool in bioimaging and for nanoscale probing.

**Keywords:** luminescence thermometry, temperature, thermal imaging, lanthanide ions, nanothermometers

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Lanthanide-based thermometers: At the cutting-edge of luminescence thermometry